

Chapter 5: Negative Numbers and Integers

Exercise 5.1 PAGE: 5.5

1. Write the opposite of each of the following:

- (i) Increase in population
- (ii) Depositing money in a bank
- (iii) Earning money
- (iv) Going North
- (v) Gaining a weight of 4kg
- (vi) A loss of Rs 1000
- (vii) 25
- (viii) – 15

Solution:

- (i) The opposite of Increase in population is Decrease in population.
- (ii) The opposite of Depositing money in a bank is Withdrawing money from a bank.
- (iii) The opposite of earning money is Spending money.
- (iv) The opposite of Going North is Going South.
- (v) The opposite of gaining a weight of 4kg is losing a weight of 4kg.
- (vi) The opposite of a loss of Rs 1000 is a gain of Rs 1000.
- (vii) The opposite of 25 is – 25.
- (viii) The opposite of – 15 is 15.

2. Indicate the following by using integers:

- (i) 25° above zero
- (ii) 5° below zero
- (iii) A profit of Rs 800
- (iv) A deposit of Rs 2500
- (v) 3km above sea level
- (vi) 2km below level

Solution:

- (i) 25° above zero is + 25°.
- (ii) 5° below zero is – 5°.
- (iii) A profit of Rs 800 is + 800.
- (iv) A deposit of Rs 2500 is + 2500.
- (v) 3km above sea level is + 3.
- (vi) 2km below level is – 2.

3. Mark the following integers on a number line:

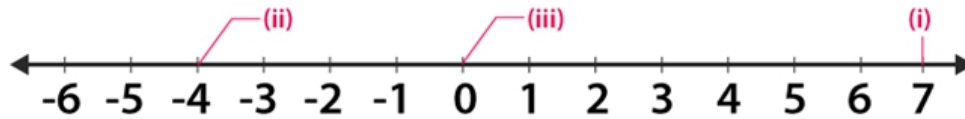
(i) 7

(ii) -4

(iii) 0

Solution:

The following integers are marked on a number line as given below:



4. Which number in each of the following pairs is smaller?

(i) 0, -4

(ii) -3, 12

(iii) 8, 13

(iv) -15, -27

Solution:

(i) 0 is greater than the negative integers

So we get $-4 < 0$

Therefore, -4 is smaller.

(ii) 12 is greater than -3 on a number line

So we get

$-3 < 12$

Therefore, -3 is smaller.

(iii) 13 is greater than 8 on a number line

So we get $8 < 13$

Therefore, 8 is smaller.

(iv) -15 is greater than -27 on a number line

So we get $-27 < -15$

Therefore, -27 is smaller.

5. Which number in each of the following pairs is larger?

(i) 3, -4

(ii) -12, -8

(iii) 0, 7

(iv) 12, -18

Solution:

(i) We know that 3 is larger than -4 on a number line

So we get $3 > -4$

Therefore, 3 is larger.

(ii) We know that -8 is larger than -12 on a number line

So we get $-8 > -12$

Therefore, -8 is larger.

(iii) We know that 7 is larger than 0 on a number line

So we get $7 > 0$

Therefore, 7 is larger.

(iv) We know that 12 is larger than -18 on a number line

So we get $12 > -18$

Therefore, 12 is larger.

6. Write all integers between:

(i) -7 and 3

(ii) -2 and 2

(iii) -4 and 0

(iv) 0 and 3

Solution:

(i) The integers between -7 and 3 are

$-6, -5, -4, -3, -2, -1, 0, 1, 2$

(ii) The integers between -2 and 2 are

$-1, 0, 1.$

(iii) The integers between -4 and 0 are

$-3, -2, -1$

(iv) The integers between 0 and 3 are

$1, 2.$

7. How many integers are between?

(i) -4 and 3

(ii) 5 and 12

(iii) -9 and -2

(iv) 0 and 5

Solution:

(i) The integers between -4 and 3 are

$-3, -2, -1, 0, 1, 2$

Therefore, number of integers between -4 and 3 are 6.

(ii) The integers between 5 and 12 are

$6, 7, 8, 9, 10, 11$

Therefore, number of integers between 5 and 12 are 6.

(iii) The integers between -9 and -2 are

$-8, -7, -6, -5, -4, -3$

Therefore, number of integers between -9 and -2 are 6 .

(iv) The integers between 0 and 5 are

$1, 2, 3, 4$

Therefore, number of integers between 0 and 5 are 4 .

8. Replace $*$ in each of the following by $<$ or $>$ so that the statement is true:

(i) $2 * 5$

(ii) $0 * 3$

(iii) $0 * -7$

(iv) $-18 * 15$

(v) $-235 * -532$

(vi) $-20 * 20$

Solution:

(i) $2 < 5$

(ii) $0 < 3$

(iii) $0 > -7$

(iv) $-18 < 15$

(v) $-235 > -532$

(vi) $-20 < 20$

9. Write the following integers in increasing order:

(i) $-8, 5, 0, -12, 1, -9, 15$

(ii) $-106, 107, -320, -7, 185$

Solution:

(i) $-8, 5, 0, -12, 1, -9, 15$ can be written in increasing order as

$-12, -9, -8, 0, 1, 5, 15$

(ii) $-106, 107, -320, -7, 185$ can be written in increasing order as

$-320, -106, -7, 107, 185$.

10. Write the following integers in decreasing order:

(i) $-15, 0, -2, -9, 7, 6, -5, 8$

(ii) $-154, 123, -205, -89, -74$

Solution:

(i) $-15, 0, -2, -9, 7, 6, -5, 8$ can be written in decreasing order as

$8, 7, 6, 0, -2, -5, -9, -15$

(ii) $-154, 123, -205, -89, -74$ can be written in decreasing order as

$123, -74, -89, -154, -205$

11. Using the number line, write the integer which is:

(i) 2 more than 3

(ii) 5 less than 3

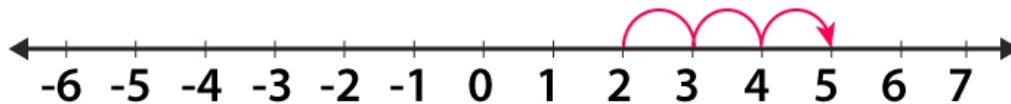
(iii) 4 more than -9

Solution:

(i) 2 more than 3

In order to get the integer 2 more than 3

We draw a number line from 2 and proceed 3 units to the right to obtain 5

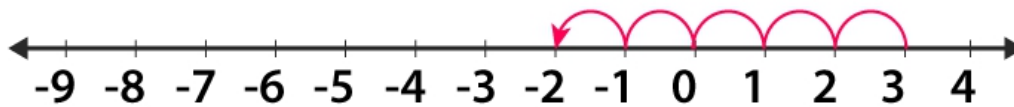


Therefore, 2 more than 3 is 5.

(ii) 5 less than 3

In order to get the integer 5 less than 3

We draw a number line from 3 and proceed 5 units to the left to obtain -2

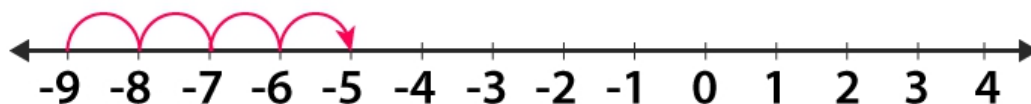


Therefore, 5 less than 3 is -2 .

(iii) 4 more than -9

In order to get the integer 4 more than -9

We draw a number line from -9 and proceed 4 units to the right to obtain -5



Therefore, 4 more than -9 is -5 .

12. Write the absolute value of each of the following:

(i) 14

(ii) -25

(iii) 0

(iv) -125

(v) -248

(vi) $a - 7$, if a is greater than 7

(vii) $a - 7$, if $a - 2$ is less than 7

(viii) $a + 4$, if a is greater than -4

(ix) $a + 4$ if a is less than -4

(x) $|-3|$

(xi) $-|-5|$

(xii) $|12 - 5|$

Solution:

(i) The absolute value of 14 is

$$|14| = 14$$

(ii) The absolute value of -25 is

$$|-25| = 25$$

(iii) The absolute value of 0 is

$$|0| = 0$$

(iv) The absolute value of -125 is

$$|-125| = 125$$

(v) The absolute value of -248 is

$$|-248| = 248$$

(vi) The absolute value of $a - 7$, if a is greater than 7 is

$$|a - 7| = a - 7 \text{ where } a > 7$$

(vii) The absolute value of $a - 7$, if $a - 2$ is less than 7 is

$$|a - 7| = -(a - 7) \text{ where } a - 2 < 7$$

(viii) The absolute value of $a + 4$, if a is greater than -4 is

$$|a + 4| = a + 4 \text{ where } a > -4$$

(ix) The absolute value of $a + 4$ if a is less than -4 is

$$|a + 4| = -(a + 4) \text{ where } a < -4$$

(x) The absolute value of $|-3|$ is

$$|-3| = 3$$

(xi) The absolute value of $-|-5|$ is

$$-|-5| = 5$$

(xii) The absolute value of $|12 - 5|$ is

$$|12 - 5| = 7$$

13. (i) Write 4 negative integers less than -10 .

(ii) Write 6 negative integers just greater than -12 .

Solution:

(i) The 4 negative integers less than -10 are

$$-11, -12, -13, -14$$

(ii) The 6 negative integers just greater than -12 are

$$-11, -10, -9, -8, -7, -6$$

14. Which of the following statements are true?

- (i) The smallest integer is zero.**
- (ii) The opposite of zero is zero.**
- (iii) Zero is not an integer.**
- (iv) 0 is larger than every negative integer.**
- (v) The absolute value of an integer is greater than the integer.**
- (vi) A positive integer is greater than its opposite.**
- (vii) Every negative integer is less than every natural number.**
- (viii) 0 is the smallest positive integer.**

Solution:

- (i) False. The smallest integer is 1.
- (ii) True. 0 is neither positive nor negative so the opposite is 0.
- (iii) False. Zero is an integer which is neither positive nor negative.
- (iv) True. 0 is larger than -1 .
- (v) False. The absolute value of an integer is the numerical value.
- (vi) True. 3 is greater than -3 .
- (vii) True. -3 is less than 1.
- (viii) False. 1 is the smallest positive integer.

Exercise 5.2 PAGE: 5.9

1. Draw a number line and represent each of the following on it:

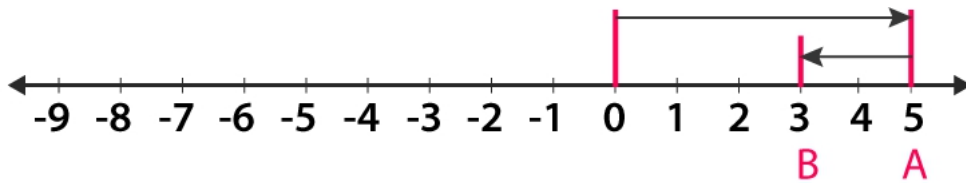
- (i) $5 + (-2)$**
- (ii) $(-9) + 4$**
- (iii) $(-3) + (-5)$**
- (iv) $6 + (-6)$**
- (v) $(-1) + (-2) + 2$**
- (vi) $(-2) + 7 + (-9)$**

Solution:

- (i) $5 + (-2)$

From 0 move towards right of first five units to obtain + 5

So the second number is -2 so move 2 units towards left of + 5 we get + 3

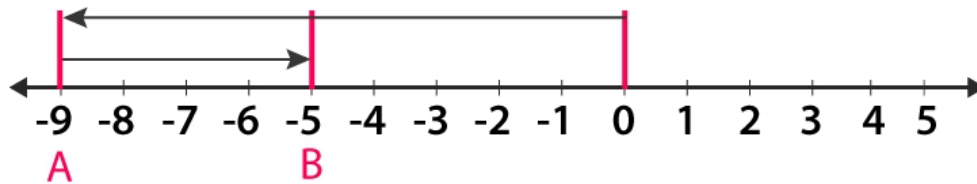


Therefore, $5 + (-2) = 3$.

(ii) $(-9) + 4$

From 0 move towards left of nine units to obtain -9

So the second number is 4 so move 4 units towards right of -9 we get -5

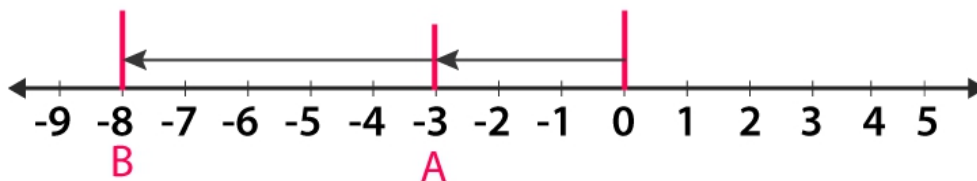


Therefore, $(-9) + 4 = -5$.

(iii) $(-3) + (-5)$

From 0 move towards left of three units to obtain -3

So the second number is -5 so move 5 units towards left of -3 we get -8



Therefore, $(-3) + (-5) = -8$.

(iv) $6 + (-6)$

From zero move towards right of six units to obtain 6

So the second number is -6 so move 6 units towards left of 6 we get 0



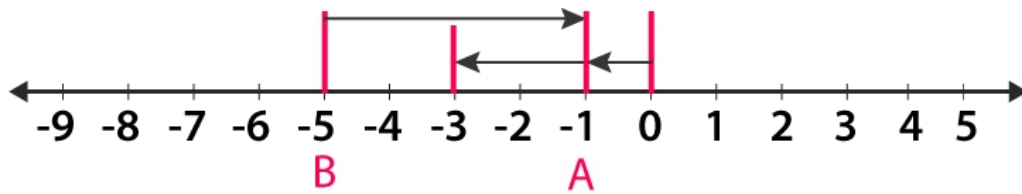
Therefore, $6 + (-6) = 0$.

(v) $(-1) + (-2) + 2$

From zero move towards left of one unit to obtain -1

So the second number is -2 so move 2 units towards left of -1 we get -3

The third number is 2 so move 2 units towards right of -3 we get -1



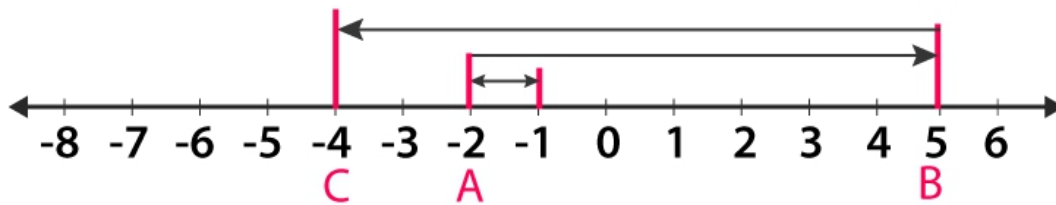
Therefore, $(-1) + (-2) + 2 = -1$.

(vi) $(-2) + 7 + (-9)$

From zero move towards left of two units to obtain -2

So the second number is 7 so move 7 units towards right of -2 we get 5

The third number is -9 so move 9 units towards left of 5 we get -4



Therefore, $(-2) + 7 + (-9) = -4$.

2. Find the sum of

(i) -557 and 488

(ii) -522 and -160

(iii) 2567 and -325

(iv) -10025 and 139

(v) 2547 and -2548

(vi) 2884 and -2884

Solution:

(i) -557 and 488

We get

$$-557 + 488$$

It can be written as

$$|-557| - |488| = 557 - 488 = 69.$$

(ii) -522 and -160

We get

$$-522 + (-160)$$

It can be written as

$$-522 - 160 = -682$$

(iii) 2567 and -325

We get

$$2567 + (-325)$$

It can be written as

$$2567 - 325 = 2242$$

(iv) -10025 and 139

We get

$$-10025 + 139$$

It can be written as

$$-10025 + 139 = -9886$$

(v) 2547 and -2548

We get

$$2547 + (-2548)$$

It can be written as

$$2547 - 2548 = -1$$

(vi) 2884 and -2884

We get

$$2884 + (-2884)$$

It can be written as

$$2884 - 2884 = 0$$

Exercise 5.3 page: 5.11

1. Find the additive inverse of each of the following integers:

(i) 52

(ii) -176

(iii) 0

(iv) 1

Solution:

(i) The additive inverse of 52 is - 52.

(ii) The additive inverse of - 176 is 176.

(iii) The additive inverse of 0 is 0.

(iv) The additive inverse of 1 is - 1.

2. Find the successor of each of the following integers:

(i) - 42

(ii) -1

(iii) 0

(iv) - 200

(v) -99

Solution:

(i) The successor of -42 is

$$-42 + 1 = -41$$

(ii) The successor of -1 is

$$-1 + 1 = 0$$

(iii) The successor of 0 is

$$0 + 1 = 1$$

(iv) The successor of -200 is

$$-200 + 1 = -199$$

(v) The successor of -99 is

$$-99 + 1 = -98$$

3. Find the predecessor of each of the following integers:

(i) 0

(ii) 1

(iii) -1

(iv) -125

(v) 1000

Solution:

(i) The predecessor of 0 is

$$0 - 1 = -1$$

(ii) The predecessor of 1 is

$$1 - 1 = 0$$

(iii) The predecessor of -1 is

$$-1 - 1 = -2$$

(iv) The predecessor of -125 is

$$-125 - 1 = -126$$

(v) The predecessor of 1000 is

$$1000 - 1 = 999$$

4. Which of the following statements are true?

(i) The sum of a number and its opposite is zero.

(ii) The sum of two negative integers is a positive integer.

(iii) The sum of a negative integer and a positive integer is always a negative integer.

(iv) The successor of -1 is 1 .

(v) The sum of three different integers can never be zero.

Solution:

- (i) True. $1 - 1 = 0$
- (ii) False. $-1 - 1 = -2$
- (iii) False. $-2 + 3 = 1$
- (iv) False. The successor of -1 is 0 .
- (v) False. $1 + 2 - 3 = 0$

5. Write all integers whose absolute values are less than 5.

Solution:

The integers whose absolute values are less than 5 are

$-4, -3, -2, -1, 0, 1, 2, 3, 4$

6. Which of the following is false:

- (i) $|4 + 2| = |4| + |2|$
- (ii) $|2 - 4| = |2| + |4|$
- (iii) $|4 - 2| = |4| - |2|$
- (iv) $|(-2) + (-4)| = |-2| + |-4|$

Solution:

- (i) True.
- (ii) False.
- (iii) True.
- (iv) True.

7. Complete the following table:

+	-6	-4	-2	0	2	4	6
6						10	
4							
2							8
0	-6						
-2							
-4						0	
-6				-6			

From the above table:

- (i) Write all the pairs of integers whose sum is 0.
- (ii) Is $(-4) + (-2) = (-2) + (-4)$?
- (iii) Is $0 + (-6) = -6$?

Solution:

+	-6	-4	-2	0	2	4	6
6	0	2	4	6	8	10	12
4	-2	0	2	4	6	8	10
2	-4	-2	0	2	4	6	8
0	-6	-4	-2	0	2	4	6
-2	-8	-6	-4	-2	0	2	4
-4	-10	-8	-6	-4	-2	0	2
-6	-12	-10	-8	-6	-4	-2	0

(i) The pairs of integers whose sum is 0 are

(6, -6), (4, -4), (2, -2), (0, 0)

(ii) Yes. By using commutativity of addition $(-4) + (-2) = (-2) + (-4)$

(iii) Yes. By using additive identity $0 + (-6) = -6$.

8. Find an integer x such that

(i) $x + 1 = 0$

(ii) $x + 5 = 0$

(iii) $-3 + x = 0$

(iv) $x + (-8) = 0$

(v) $7 + x = 0$

(vi) $x + 0 = 0$

Solution:

(i) $x + 1 = 0$

Subtracting 1 on both sides

$$x + 1 - 1 = 0 - 1$$

We get

$$x = -1$$

(ii) $x + 5 = 0$

By subtracting 5 on both sides

$$x + 5 - 5 = 0 - 5$$

So we get

$$x = -5$$

(iii) $-3 + x = 0$

By adding 3 on both sides

$$-3 + x + 3 = 0 + 3$$

So we get

$$x = 3$$

(iv) $x + (-8) = 0$

By adding 8 on both sides

$$x - 8 + 8 = 0 + 8$$

So we get

$$x = 8$$

(v) $7 + x = 0$

By subtracting 7 on both sides

$$7 + x - 7 = 0 - 7$$

So we get

$$x = -7$$

(vi) $x + 0 = 0$

So we get

$$x = 0$$

Exercise 5.4 page: 5.17

1. Subtract the first integer from the second in each of the following:

(i) 12, -5

(ii) -12, 8

(iii) -225, -135

(iv) 1001, 101

(v) -812, 3126

(vi) 7560, -8

(vii) -3978, -4109

(viii) 0, -1005

Solution:

(i) 12, -5

So by subtracting the first integer from the second

$$-5 - 12 = -17$$

(ii) -12, 8

So by subtracting the first integer from the second

$$8 - (-12) = 8 + 12 = 20$$

(iii) -225, -135

So by subtracting the first integer from the second

$$-135 - (-225) = 225 - 135 = 90$$

(iv) 1001, 101

So by subtracting the first integer from the second

$$101 - 1001 = -900$$

(v) $-812, 3126$

So by subtracting the first integer from the second

$$3126 - (-812) = 3126 + 812 = 3938$$

(vi) $7560, -8$

So by subtracting the first integer from the second

$$-8 - 7560 = -7568$$

(vii) $-3978, -4109$

So by subtracting the first integer from the second

$$-4109 - (-3978) = -4109 + 3978 = -131$$

(viii) $0, -1005$

So by subtracting the first integer from the second

$$-1005 - 0 = -1005$$

2. Find the value of:

(i) $-27 - (-23)$

(ii) $-17 - 18 - (-35)$

(iii) $-12 - (-5) - (-125) + 270$

(iv) $373 + (-245) + (-373) + 145 + 3000$

(v) $1 + (-475) + (-475) + (-475) + (-475) + 1900$

(vi) $(-1) + (-304) + 304 + 304 + (-304) + 1$

Solution:

(i) $-27 - (-23)$

So we get

$$= -27 + 23$$

On further calculation

$$= 23 - 27$$

We get

$$= -4$$

(ii) $-17 - 18 - (-35)$

So we get

$$= -35 + 35$$

On further calculation

$$= 0$$

(iii) $-12 - (-5) - (-125) + 270$

So we get

$$= -12 + 5 + 125 + 270$$

On further calculation

$$= 400 - 12$$

We get

$$= 388$$

$$(iv) 373 + (-245) + (-373) + 145 + 3000$$

So we get

$$= 373 - 245 - 373 + 145 + 3000$$

On further calculation

$$= 3145 + 373 - 373 - 245$$

We get

$$= 3145 - 245$$

By subtraction

$$= 2900$$

$$(v) 1 + (-475) + (-475) + (-475) + (-475) + 1900$$

So we get

$$= 1 - 950 - 950 + 1900$$

On further calculation

$$= 1900 + 1 - 1900$$

We get

$$= 1$$

$$(vi) (-1) + (-304) + 304 + 304 + (-304) + 1$$

So we get

$$= -1 + 1 - 304 + 304 - 304 + 304$$

On further calculation

$$= 0$$

3. Subtract the sum of - 5020 and 2320 from - 709.

Solution:

We know that the sum of -5020 and 2320 is

$$-5020 + 2320$$

It can be written as

$$= 2320 - 5020$$

So we get

$$= -2700$$

Subtracting from - 709 we get

$$= -709 - (-2700)$$

We get

$$= -709 + 2700$$

By subtraction

$$= 1991$$

4. Subtract the sum of -1250 and 1138 from the sum of 1136 and -1272 .

Solution:

We know that the sum of -1250 and 1138 is

$$-1250 + 1138$$

It can be written as

$$= 1138 - 1250$$

So we get

$$= -112$$

We know that the sum of 1136 and -1272 is

$$1136 - 1272 = -136$$

So we get

$$-136 - (-112) = -136 + 112 = -24$$

5. From the sum of 233 and -147 , subtract -284 .

Solution:

We know that the sum of 233 and -147 is

$$233 - 147 = 86$$

Subtracting -284 we get

$$86 - (-284) = 86 + 284 = 370$$

6. The sum of two integers is 238 . If one of the integers is -122 , determine the other.

Solution:

It is given that

$$\text{Sum of two integers} = 238$$

$$\text{One of the integers} = -122$$

$$\text{So the other integer} = -(-122) + 238$$

On further calculation

$$\text{Other integer} = 238 + 122 = 360$$

7. The sum of two integers is -223 . If one of the integers is 172 , find the other.

Solution:

It is given that

$$\text{Sum of two integers} = -223$$

$$\text{One of the integers} = 172$$

$$\text{So the other integer} = -223 - 172 = -395$$

8. Evaluate the following:

(i) $- 8 - 24 + 31 - 26 - 28 + 7 + 19 - 18 - 8 + 33$

(ii) $- 26 - 20 + 33 - (-33) + 21 + 24 - (-25) - 26 - 14 - 34$

Solution:

(i) $- 8 - 24 + 31 - 26 - 28 + 7 + 19 - 18 - 8 + 33$

We get

$$= - 8 - 24 - 26 - 28 - 18 - 8 + 31 + 7 + 19 + 33$$

On further calculation

$$= - 32 - 26 - 28 - 26 + 38 + 19 + 33$$

It can be written as

$$= 38 - 32 - 26 - 28 + 33 - 26 + 19$$

So we get

$$= 6 - 26 - 28 + 7 + 19$$

By calculation

$$= 6 - 28 - 26 + 26$$

$$= 6 - 28$$

By subtraction

$$= - 22$$

(ii) $- 26 - 20 + 33 - (-33) + 21 + 24 - (-25) - 26 - 14 - 34$

We get

$$= - 46 + 33 + 33 + 21 + 24 + 25 - 26 - 14 - 34$$

On further calculation

$$= - 46 + 66 + 21 + 24 + 25 + (-74)$$

It can be written as

$$= - 46 + 66 + 70 - 74$$

So we get

$$= - 46 - 4 + 66$$

By calculation

$$= - 50 + 66$$

$$= 66 - 50$$

By subtraction

$$= 16$$

9. Calculate

$1 - 2 + 3 - 4 + 5 - 6 + \dots + 15 - 16$

Solution:

It can be written as

$$1 - 2 + 3 - 4 + 5 - 6 + 7 - 8 + 9 - 10 + 11 - 12 + 13 - 14 + 15 - 16$$

We get

$$= -1 - 1 - 1 - 1 - 1 - 1 - 1 - 1$$

By calculation

$$= -8$$

10. Calculate the sum:

$$5 + (-5) + 5 + (-5) + \dots$$

(i) if the number of terms is 10.

(ii) if the number of terms is 11.

Solution:

(i) if the number of terms is 10

We get

$$5 + (-5) + 5 + (-5) + 5 + (-5) + 5 + (-5) + 5 + (-5)$$

On further calculation

$$= 5 - 5 + 5 - 5 + 5 - 5 + 5 - 5 + 5 - 5 = 0$$

(ii) if the number of terms is 11

We get

$$5 + (-5) + 5 + (-5) + 5 + (-5) + 5 + (-5) + 5 + (-5) + 5$$

On further calculation

$$= 5 - 5 + 5 - 5 + 5 - 5 + 5 - 5 + 5 - 5 + 5 = 5$$

11. Replace * by < or > in each of the following to make the statement true:

(i) $(-6) + (-9) * (-6) - (-9)$

(ii) $(-12) - (-12) * (-12) + (-12)$

(iii) $(-20) - (-20) * 20 - (65)$

(iv) $28 - (-10) * (-16) - (-76)$

Solution:

(i) $(-6) + (-9) < (-6) - (-9)$

(ii) $(-12) - (-12) > (-12) + (-12)$

(iii) $(-20) - (-20) > 20 - (65)$

(iv) $28 - (-10) < (-16) - (-76)$

12. If Δ is an operation on integers such that $a \Delta b = -a + b - (-2)$ for all integers a, b. Find the value of

(i) $4 \Delta 3$

(ii) $(-2) \Delta (-3)$

(iii) $6 \Delta (-5)$

(iv) $(-5) \Delta 6$

Solution:

(i) $4 \triangle 3$

By substituting values in $a \triangle b = -a + b - (-2)$

We get

$$4 \triangle 3 = -4 + 3 - (-2) = 1$$

(ii) $(-2) \triangle (-3)$

By substituting values in $a \triangle b = -a + b - (-2)$

We get

$$(-2) \triangle (-3) = -(-2) + (-3) - (-2) = 1$$

(iii) $6 \triangle (-5)$

By substituting values in $a \triangle b = -a + b - (-2)$

We get

$$6 \triangle (-5) = -6 + (-5) - (-2) = -9$$

(iv) $(-5) \triangle 6$

By substituting values in $a \triangle b = -a + b - (-2)$

We get

$$(-5) \triangle 6 = -(-5) + 6 - (-2) = 13$$

13. If a and b are two integers such that a is the predecessor of b. Find the value of a – b.

Solution:

It is given that a is the predecessor of b

We can write it as

$$a + 1 = b$$

So we get

$$a - b = -1$$

14. If a and b are two integers such that a is the successor of b. Find the value of a – b.

Solution:

It is given that a is the successor of b

We can write it as

$$a - 1 = b$$

So we get

$$a - b = 1$$

15. Which of the following statements are true:

(i) $-13 > -8 - (-2)$

(ii) $-4 + (-2) < 2$

(iii) The negative of a negative integer is positive.

- (iv) If a and b are two integers such that $a > b$, then $a - b$ is always a positive integer.
- (v) The difference of two integers is an integer.
- (vi) Additive inverse of a negative integer is negative.
- (vii) Additive inverse of a positive integer is negative.
- (viii) Additive inverse of a negative integer is positive.

Solution:

- (i) False.
- (ii) True.
- (iii) True.
- (iv) True.
- (v) True.
- (vi) False.
- (vii) True.
- (viii) True.

16. Fill in the blanks:

- (i) $-7 + \dots = 0$
- (ii) $29 + \dots = 0$
- (iii) $132 + (-132) = \dots$
- (iv) $-14 + \dots = 22$
- (v) $-1256 + \dots = -742$
- (vi) $\dots - 1234 = -4539$

Solution:

- (i) $-7 + 7 = 0$
- (ii) $29 + (-29) = 0$
- (iii) $132 + (-132) = 0$
- (iv) $-14 + 36 = 22$
- (v) $-1256 + 514 = -742$
- (vi) $-3305 - 1234 = -4539$

Objective Type Questions page: 5.18

Mark the correct alternative in each of the following:

1. Which of the following statement is true?

- (a) $-7 > -5$
- (b) $-7 < -5$
- (c) $(-7) + (-5) > 0$
- (d) $(-7) - (-5) > 0$

Solution:

The option (b) is correct answer.

In option (a)

We know that -7 is to the left of -5

Hence, $-7 < -5$.

In option (c)

We know that $(-7) + (-5) = -(7 + 5) = -12$.

So -12 is to the left of 0

Hence $(-7) + (-5) < 0$.

In option (d)

$(-7) - (-5) = (-7) + (\text{additive inverse of } -5) = (-7) + (5) = -(7 - 5) = -2$

We know that -2 is to the left of 0 , so $(-7) - (-5) < 0$.

2. 5 less than -2 is

(a) 3

(b) -3

(c) -7

(d) 7

Solution:

The option (c) is correct answer.

We know that, 5 less than $-2 = (-2) - (5) = -2 - 5 = -7$

3. 6 more than -7 is

(a) 1

(b) -1

(c) 13

(d) -13

Solution:

The option (b) is correct answer.

We know that, 6 more than $-7 = (-7) + 6 = -(7 - 6) = -1$

4. If x is a positive integer, then

(a) $x + |x| = 0$

(b) $x - |x| = 0$

(c) $x + |x| = -2x$

(d) $x = -|x|$

Solution:

The option (b) is correct answer.

We know that if x is positive integer, then $|x| = x$

Hence, $x + |x| = x + x = 2x$ and $x - |x| = x - x = 0$

5. If x is a negative integer, then

(a) $x + |x| = 0$

(b) $x - |x| = 0$

(c) $x + |x| = 2x$

(d) $x - |x| = -2x$

Solution:

The option (a) is correct answer.

We know that x is negative integer, then $|x| = -x$

It can be written as

$x + |x| = x - x = 0$ and $x - |x| = x - (-x) = x + x = 2x$

6. If x is greater than 2, then $|2 - x| =$

(a) $2 - x$

(b) $x - 2$

(c) $2 + x$

(d) $-x - 2$

Solution:

The option (b) is correct answer.

We know that if a is negative integer, then $|a| = -a$

It is given that x is greater than 2 where $2 - x$ is negative

Hence, $|2 - x| = -(2 - x) = -2 + x = x - 2$.

7. $9 + |-4|$ is equal to
(a) 5 (b) -5 (c) 13 (d) -13

Solution:

The option (c) is correct answer.

We know that, $|-4| = 4$

Hence $9 + |-4| = 9 + 4 = 13$

8. $(-35) + (-32)$ is equal to
(a) 67 (b) -67 (c) -3 (d) 3

Solution:

The option (b) is correct answer.

It can be written as $(-35) + (-32) = -(35 + 32) = -67$

9. $(-29) + 5$ is equal to
(a) 24 (b) 34 (c) -34 (d) -24

Solution:

The option (d) is correct answer.

It can be written as $(-29) + 5 = -(29 - 5) = -24$

10. $|-|-7| - 3|$ is equal to
(a) -7 (b) 7 (c) 10 (d) -10

Solution:

The option (c) is correct answer.

It can be written as $|-|-7| - 3| = |-7 - 3| = |-10| = 10$

11. The successor of -22 is
(a) -23 (b) -21 (c) 23 (d) 21

Solution:

The option (b) is correct answer.

We know that if 'a' is an integer $a + 1$ is its successor.

So the successor of $-22 = -22 + 1 = -(22 - 1) = -21$

12. The predecessor of -14 is
(a) -15 (b) 15 (c) 13 (d) -13

Solution:

The option (a) is correct answer.

The predecessor of -14 is -15 .

13. If the sum of two integers is -26 and one of them is 14, then the other integer is
(a) -12 (b) 12 (c) -40 (d) 40

Solution:

The option (c) is correct answer.

It is given that the sum of two integers = - 26

One of them = 14

So the other integer = - 26 - 14 = - (26 + 14) = - 40

14. Which of the following pairs of integers have 5 as a difference?

- (a) 10, 5 (b) - 10, - 5 (c) 15, - 20 (d) both (a) and (b)

Solution:

The option (d) is correct answer.

Consider option (a) $10 - 5 = 5$

Consider option (b) $(- 5) - (- 10) = - 5 + 10 = 5$

Consider option (c) $15 - (- 20) = 15 + 20 = 35$

15. If the product of two integers is 72 and one of them is - 9, then the other integers is

- (a) - 8 (b) 8 (c) 81 (d) 63

Solution:

The option (a) is correct answer.

It is given that the product of two integers = 72

One of them = - 9

Hence, the other integers = $72 \div (- 9) = - 8$

16. On subtracting - 7 from - 14, we get

- (a) - 12 (b) - 7 (c) -14 (d) 21

Solution:

The option (b) is correct answer.

It can be written as

Required number = $- 14 - (- 7) = - 14 + 7 = - (14 - 7) = - 7$

17. The largest number that divides 64 and 72 and leave the remainders 12 and 7 respectively, is

- (a) 17 (b) 13 (c) 14 (d) 18

Solution:

The option (b) is correct answer.

By subtracting 12 and 7 from 64 and 72

We get

$64 - 12 = 52$ and $72 - 7 = 65$

So the required number is the HCF of 52 and 65.

It can be written as

$52 = 4 \times 13$ and $65 = 5 \times 13$

HCF of 52 and 65 = 13

Hence, the largest number that divides 64 and 72 and leave the remainders 12 and 7 respectively, is 13.

18. The sum of two integers is - 23. If one of them is 18, then the other is
(a) -14 (b) 14 (c) 41 (d) -41

Solution:

The option (d) is correct answer.

It is given as the sum of two integers = - 23

One of them = 18

So the other number = $(- 23) - (18) = - 23 - 18 = - (23 + 18) = - 41$

Hence, the other number is - 41.

19. The sum of two integers is - 35. If one of them is 40, then the other is
(a) 5 (b) - 75 (c) 75 (d) - 5

Solution:

The option (b) is correct answer.

It is given that the sum of two integers = - 35

One of them = 40

So the other number = $(- 35) - (40) = - 35 - 40 = - (35 + 40) = - 75$

Hence, the other number is - 75.

20. On subtracting - 5 from 0, we get
(a) - 5 (b) 5 (c) 50 (d) 0

Solution:

The option (b) is correct answer.

We know that, $0 - (- 5) = 0 + 5 = 5$

Hence by subtracting - 5 from 0, we obtain 5.

21. $(- 16) + 14 - (- 13)$ is equal to
(a) - 11 (b) 12 (c) 11 (d) - 15

Solution:

The option (c) is correct answer.

It can be written as $(- 16) + 14 - (- 13) = (- 16) + 14 + 13 = (- 16) + 27 = 27 - 16 = 11$

22. $(- 2) \times (- 3) \times 6 \times (- 1)$ is equal to
(a) 36 (b) - 36 (c) 6 (d) - 6

Solution:

The option (b) is correct answer.

It can be written as $(- 2) \times (- 3) \times 6 \times (- 1) = (2 \times 3) \times 6 \times (- 1) = 6 \times 6 \times (- 1) = 36 \times (- 1)$

So we get $(- 2) \times (- 3) \times 6 \times (- 1) = - (36 \times 1) = - 36$

23. $86 + (- 28) + 12 + (- 34)$ is equal to
(a) 36 (b) - 36 (c) 6 (d) - 6

Solution:

The option (a) is correct answer.

It can be written as $86 + (-28) + 12 + (-34) = 86 + (-28) - (34 - 12) = 86 + (-28) - 22$

On further calculation

$$86 + (-28) + 12 + (-34) = (86 - 28) - (34 - 12) = (86 - 28) - 22 = 58 - 22 = 36$$

24. $(-12) \times (-9) - 6 \times (-8)$ is equal to

(a) 156

(b) 60

(c) -156

(d) - 60

Solution:

The option (a) is correct answer.

It can be written as $(-12) \times (-9) - 6 \times (-8) = (12 \times 9) - 6 \times (-8) = 108 - 6 \times (-8)$

On further calculation

$$(-12) \times (-9) - 6 \times (-8) = 108 + 6 \times 8 = 108 + 48 = 156$$